MASSACHUSETTS INSTITUTE OF TECHNOLOGY DEPARTMENT OF OCEAN ENGINEERING AND CIVIL AND ENVIRONMENTAL ENGINEERING 13.10J/1.573J Structural Mechanics Fall 2001

Quiz 2

6:00pm - 8:00pm Thursday, November 15, 2001 Room 3-370

CLOSED BOOK & NOTES, TWO SHEETS OF FORMULAS FIRST, READ ALL THREE PROBLEMS !!! INDIVIDUAL EFFORT 1. (25pts) The normal strains at a point P along directions 1,2 and 3 on the planar surface of a linearly elastic thin plate with Young's modulus of elasticity E = 200GPa and Poisson's ratio $\nu = 0.3$ are measured as shown in Figure 1. Note that due to Poisson effect there may exist strain orthogonal to the xy plane.



Figure 1: Problem 1

- (a) (15pts) Find ϵ_{xy} and then find the principal strains and their directions.
- (b) (10pts) Describe a method to determine the principal stresses and their directions but do not carry out the algebra.

(40pts) The structure shown in Figure 2 is proposed as a calibration fixture for an experiment. The cantilevered beam DF has an inverted "T-shape" *rigid* bracket attached to its tip F, as shown in Figure 2, allowing the placement of the point load P at any location along ABC.



Figure 2: Problem 2-a

- (a) (9pts) Assuming that the bending rigidity of the beam DF is EI, sketch the resulting shear force and bending moment diagrams for the beam DF for the load placed at A, B and C. Indicate the positions and values of the maximum bending moments for each case.
- (b) (18pts) A point load P is acting at C in the negative y direction and another point load P is acting at F in the positive z direction, as shown in Figure 3.
 - i. (**9pts**) Find the neutral axis at the position where the maximum bending moment occurs.
 - ii. (9pts) Find the maximum normal stress τ_{xx} .



Figure 3: Problem 2-b

(c) (23pts) The same beam structure with the same loads as shown in Figure 3 is considered. However, the cross section of the beam DF consists of two different materials as shown in Figure 4,



Figure 4: Problem 2-c

- i. (10pts) Find the neutral axis at the position where the maximum bending moment occurs.
- ii. (13pts) Find the maximum normal stress τ_{xx} .

3. (10pts) A rigid beam RT is supported by three steel rods as shown in Figure 5. A point load P is applied at location x on the beam RT. Assume that gravity effects can be neglected and the three bars display linearly-elastic behavior. Young's modulus of elasticity E, the cross sectional area A and the length L of the three bars are indicated in the figure, respectively. While the three rods are elastic, find the position x so that the beam remains horizontal.



Figure 5: Problem 3

4. (25pts) A rigid beam RT is supported by two steel rods as shown in Figure 6. A point force P is acting downward at the position $x = \frac{8}{5}L$. The bars are idealized to be linearly-elastic, perfectly plastic as shown in Figure 6. The midpoint Q is deflected $\frac{7\tau_y L}{3E}$ downwards by the slow application of the force P, after which the force is slowly removed. (Hint: Remember that when a material becomes plastic, no increase of force is required to get additional deformation. Also when the midpoint is deflected $\frac{7\tau_y L}{3E}$ it is **NOT** necessary that both rods are plastic.)



Figure 6: Problem 4

- (a) (10pts) What is the required maximum value of *P*?
- (b) (15pts) Find the final position of the beam after the force is removed.